

1 In the claims:

2 1. A method for gamut mapping of an input image using a space varying
3 algorithm, comprising:

4 receiving the input image;

5 converting color representations of an image pixel set to produce a corresponding
6 electrical values set;

7 applying the space varying algorithm to the electrical values set to produce a
8 color-mapped value set; and

9 reconverting the color-mapped value set to an output image.

10 2. ~~The method of claim 1, wherein the space varying algorithm minimizes a~~
11 variational problem represented by:

12
$$E(u) = \int_{\Omega} (D^2 + \alpha |\nabla D|^2) d\Omega, \text{ subject to } u \in \mathcal{G}, \text{ wherein } \Omega \text{ is a support of the input}$$

13 image, α is a non-negative real number, $D = g * (u - u_0)$, g is a normalized Gaussian kernel
14 with zero mean and a small variance σ , u_0 is the input image, and u is the output image.

15 3. The method of claim 2, further comprising:

16 solving the variational problem at a high value of α ;

17 solving the variational problem at a low value of α ; and

18 averaging the solutions.

19 4. The method of claim 3, wherein the step of averaging the solutions comprises
20 using a spatially adaptive weighting scheme, comprising:

$$u_{final}[k, j] = w[k, j]u_{small}[k, j] + (1 - w[k, j])u_{high}[k, j],$$

21 wherein the weight $w[k, j]$, comprises:

$$w[k, j] = \frac{1}{1 + \beta |\nabla g * u_0|^2}, \text{ and}$$

22 wherein β is a non-negative real number.

23 5. The method of claim 2, wherein the variational problem is solved according to:

24
$$\frac{du}{dt} = \alpha g * \Delta D - g * D, \text{ subject to } u \in \mathcal{G}.$$

25 6. ~~The method of claim 2, wherein the space varying algorithm is solved according~~
26 ~~to:~~

1

$$u_{ij}^{n+1} = u_{ij}^n + \tau (\alpha L_{ij}^n - \overline{D_{ij}^n}), \text{ subject to } u_{ij}^n \in \mathcal{D}, \text{ wherein}$$

$$\tau = dt,$$

2

$$\overline{D^n} = g * g * (u^n - u_0)$$

$$L^n = D_2 * (u^n - u_0) \text{ and}$$

$$D_2 = g_x * g_x + g_y * g_y$$

3

7. The method of claim 1, wherein the space varying algorithm minimizes a variational problem represented by:

5

$$E(u) = \int_{\Omega} (\rho_1(D) + \alpha \rho_2(|\nabla D|)) d\Omega, \text{ subject to } u \in \mathcal{D}, \text{ wherein } \rho_1 \text{ and } \rho_2 \text{ are scalar}$$

6

functions.

7

8. The method of claim 2, further comprising:

8

decimating the input image to create one or more resolution layers, wherein the

9

one or more resolution layers comprises an image pyramid; and

10

solving the variational problem for each of the one or more resolution layers.

11

9. The method of claim 1, wherein the method is executed in a camera.

12

~~10. The method of claim 1, wherein the method is executed in a printer.~~

13

11. A method for color gamut mapping, comprising:

14

converting first colorimetric values of an input image to second colorimetric

15

values of an output device, wherein output values are constrained within a gamut of the output device; and

17

using a space varying algorithm that solves an image difference problem.

18

12. A computer-readable memory for color gamut mapping, comprising an instruction set for executing color gamut mapping steps, the steps, comprising:

20

converting first colorimetric values of an original image to second colorimetric

21

values, wherein output values are constrained within a gamut of the output device; using a space varying algorithm that solves an image difference problem; and

22

optimizing a solution to the image difference problem.

23

~~13. The computer-readable memory of claim 12, wherein the image difference problem is represented by:~~

25

$$E(u) = \int_{\Omega} (D^2 + \alpha |\nabla D|^2) d\Omega$$

26

subject to $u \in \mathcal{S}$, wherein Ω is a support of an input image, α is a non-negative real number, $D = g * (u - u_0)$, g is a normalized Gaussian kernel with zero mean and small variance σ , u_0 is the input image, and u is an output image.

14. The computer-readable memory of claim 12, wherein the instruction set further comprises steps for:

- solving the image difference problem at a high value of α ;
- solving the image difference problem at a low value of α ; and
- averaging the solutions.

15. The computer-readable memory of claim 14, wherein averaging the solutions comprises using a spatially adaptive weighting scheme, comprising:

$$u_{final}[k, j] = w[k, j]u_{small}[k, j](1 - w[k, j])u_{high}[k, j], \text{ and}$$

wherein the weight $w[k, j]$, comprises:

$$w[k, j] = \frac{1}{1 + \beta |\nabla g * u_0|^2}, \text{ and}$$

wherein β is a non-negative real number.

16. The computer-readable memory of claim 12, wherein the image difference problem is represented by:

$$E(u) = \int_{\Omega} (\rho_1(D) + \alpha \rho_2(|\nabla D|)) d\Omega, \text{ wherein } \rho_1 \text{ and } \rho_2 \text{ are scalar functions.}$$

17. The computer-readable memory of claim 12, wherein the instruction set further comprises steps for:

- decimating the input image to create one or more resolution layers, wherein the one or more resolution layers comprise an image pyramid; and
- solving the image difference problem for each of the one or more resolution layers.

18. The computer-readable memory of claim 17, wherein the instruction set further comprises steps for:

- (a) initializing a first resolution layer;
- (b) calculating a gradient G for the resolution layer, the gradient G comprising:

1 $G = \Delta(u - u_o) + \alpha_k(u - u_o)$, wherein Δx is a convolution of each color

2 plane of x with $K_{LAP} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -2 & 1 \\ 0 & 1 & 0 \end{bmatrix}$ and $\alpha_k = \alpha_o * 2^{2(k-1)}$;

3 (c) calculating a normalized steepest descent value $L_j = L_{j-1} - \mu_o * \mu_{NSD} * G$, wherein
4 μ_o is a constant;

5 (d) projecting the value onto constraints $Proj_9(L_j)$, wherein $Proj_9(x)$ is a projection
6 of x into a gamut 9; and

7 (e) for a subsequent resolution layer, repeating steps (b) – (d).

8 19. A method for image enhancement using gamut mapping, comprising:

9 receiving a input image;

10 from the input image, constructing an image pyramid having a plurality of
11 resolution layers;

12 processing each resolution layer, wherein the processing includes completing a
13 gradient iteration, by:

14 calculating a gradient G ;

15 completing a gradient descent iteration; and

16 projecting the completed gradient descent iteration onto constraints; and

17 computing an output image using the processed resolution layers.

18 20. The method of claim 19, wherein the gradient G , comprises:

19
$$G = \Delta(u - u_o) + \alpha_k(u - u_o),$$

20 wherein u is the output image, u_o is the input image, and α is a non-negative real
21 number.

22 21. The method of claim 19, wherein completing the gradient descent iteration
23 comprises calculating:

24
$$\mu_{NSD} = \frac{\sum G^2}{(\sum(G * \Delta G) + \alpha_k \sum G^2)}; \text{ and}$$

25
$$L_j = L_{j-1} - \mu_o \cdot \mu_{NSD} \cdot G,$$

26 wherein μ_{NSD} is a normalized steepest descent parameter, μ_o is a constant, k is a number
27 of resolution layers in the image pyramid, and j is a specific resolution layer.

28 22. The method of claim 19, wherein projecting the completed gradient descent
29 iteration onto the constraints is given by:

$$L_j = \text{Proj}_{\mathcal{G}}(L_j),$$

wherein $\text{Proj}_{\mathcal{G}}(x)$ is a projection of x into a gamut \mathcal{G} .

23. The method of claim 19, wherein constructing the image pyramid, comprises:
smoothing the input image with a Gaussian kernel;
decimating the input image; and
setting initial conductive $L_0 = \max\{S_p\}$, wherein S_p is an image with the coarsest resolution layer for the image pyramid.

24. The method of claim 23, wherein the Gaussian kernel, comprises:

$$K_{PYR} = \begin{bmatrix} \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \\ \frac{1}{8} & \frac{1}{4} & \frac{1}{8} \\ \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \end{bmatrix}$$

25. The method of claim 19, wherein processing each resolution layer further comprises applying a space varying algorithm to minimize a variational problem represented by:

$$E(u) = \int_{\Omega} (D^2 + \alpha |\nabla D|^2) d\Omega, \text{ subject to } u \in \mathcal{G}, \text{ wherein } \Omega \text{ is a support of the}$$

image, and $D = g * (u - u_0)$, wherein g is a normalized Gaussian kernel with zero mean and small variance σ , u_0 is the input image, u is the output image, and wherein α is a non-negative real number.

26. The method of claim 19, wherein processing each resolution layer comprises applying a space varying algorithm to minimize a variational problem represented by:

$$E(u) = \int_{\Omega} (\rho_1(D) + \alpha \rho_2(|\nabla D|)) d\Omega, \text{ subject to } u \in \mathcal{G}, \text{ wherein } \rho_1 \text{ and } \rho_2$$

are scalar functions.

27. The method of claim 26, wherein ρ_1 and ρ_2 are chosen from the group

comprising $\rho(x) = |x|$ and $\rho(x) = \sqrt{1 + x^2}$.